
$\begin{array}{lllllll}1 & 11 & 21 & 31 & 41 & 51\end{array}$
$\begin{array}{llllll}3 & 13 & 23 & 33 & 43 & 53\end{array}$
$\begin{array}{llllll}5 & 15 & 25 & 35 & 45 & 55\end{array}$
$\begin{array}{llllll}7 & 17 & 27 & 37 & 47 & 57\end{array}$
$\begin{array}{llllll}9 & 19 & 29 & 39 & 49 & 59\end{array}$


आ ल Fant
 $\begin{array}{llllll}4 & 13 & 22 & 31 & 44 & 53\end{array}$ $\begin{array}{llllll}5 & 14 & 23 & 36 & 45 & 54\end{array}$ $\begin{array}{llllll}6 & 15 & 28 & 37 & 46 & 55\end{array}$ $\begin{array}{llllll}7 & 20 & 29 & 38 & 47 & 60\end{array}$ $122130 \quad 39 \quad 52$ * *

 $\begin{array}{llllll}16 & 21 & 26 & 31 & 52 & 57\end{array}$ $\begin{array}{llllll}17 & 22 & 27 & 48 & 53 & 58\end{array}$ $\begin{array}{llllll}18 & 23 & 28 & 49 & 54 & 59\end{array}$ $\begin{array}{llllll}19 & 24 & 29 & 50 & 55 & 60\end{array}$ $\begin{array}{lllll}20 & 25 & 30 & 51 & 56\end{array}$

 $\begin{array}{llllll}2 & 11 & 22 & 31 & 42 & 51\end{array}$ $\begin{array}{llllll}3 & 14 & 23 & 34 & 43 & 54\end{array}$ $\begin{array}{llllll}6 & 15 & 26 & 35 & 46 & 55\end{array}$ $\begin{array}{llllll}7 & 18 & 27 & 38 & 47 & 58\end{array}$ $\begin{array}{llllll}10 & 19 & 30 & 39 & 50 & 59\end{array}$

 $\begin{array}{llllll}8 & 13 & 26 & 31 & 44 & 57\end{array}$ $\begin{array}{llllll}9 & 14 & 27 & 40 & 45 & 58\end{array}$ $\begin{array}{llllll}10 & 15 & 28 & 41 & 46 & 59\end{array}$ $\begin{array}{llllll}11 & 24 & 29 & 42 & 47 & 60\end{array}$ $\begin{array}{llllll}12 & 25 & 30 & 43 & 56\end{array}$


## INSTRUCTIONS :

THESE 6 CARDS ARE SPECIAL!


## WITH THEM YOU CAN "MAGICALLY" FIND SOMEONE'S "SECRET NUMBER"; AMAZING YOUR FRIENDS AND FAMILY!

## HOW TO DO THE MAGIC :

1. Choose a Volunteer and ask them to select a 'Secret Number' between 1 and 60.
2. Show the Volunteer the 6 cards and ask them to select the cards that have the 'Secret Number' printed on them.
3. The Volunteer selects the card(s) that contain the 'Secret Number'.
4. The Magician looks at the selected card(s) and announces the 'Secret Number'.

## THE REAL "MAGIC" :

In Step 4 the Magician adds up the upper-left numbers of the selected card(s). (The upper-left number will be a $1,2,4,8,16$, or 32 .)

That Sum will be the volunteer's 'Secret Number'.

## PRETTY COOL TRICK :



If you want to know HOW and WHY this "magically" happens - The Explanation Pages which follow, will TELL ALL ...

Go to jorgezimmerman.org and select 'Magic Cards, Explained' for hyperlinks and video.

## EXPLANATION OF HOW and WHY IT WORKS : click for Help with NUMBERS.

Introduction: ... numbers in different Bases (a number with a subscript)
Our numbering system is in what is called BASE 10. There are 10 symbols that can represent any number. Perhaps, we like 10 because that is how many fingers and thumbs we have! It is often called a "Decimal System", because there are 10 possible symbols, (Latin 'Deci' = 10).

The BASE 10 symbols are:

$$
0,1,2,3,4,5,6,7,8 \& 9
$$

A BASE 10 number looks like 560810: - The 'Place Value' is greater moving to the left. We do not normally put the subscript 10 after the number, we assume base 10. " $5608_{10}$ " is saying that you take $5 \times 1000$, and add it to $6 \times 100$, and add it to $0 \times 10$, and add it to $8 \times 1$. We say that the value of $5608{ }_{10}$ is five thousand, six hundred, and eight.


A numbering system often used with computers is called BASE 2. There are 2 symbols that can represent any number. It is often called a "Binary System", because there are 2 possible symbols. (Latin 'Bi' $=2$ )

The_BASE 2 symbols are:

## 0 \& 1

Sometimes 0 \& 1 represent opposites: No/Yes, False/True, Off/On, Wrong/Right, Down/Up, Right/Left, Black/White ... and so on.
A BASE 2 number looks like 11012: - The 'Place Value' is greater moving to the left " $1101_{2}$ " is saying that you take $1 \times 8$ and add it to $1 \times 4$ and add it to $0 \times 2$ and add it to $1 \times 1$. We say that the decimal value of 11012 is thirteen.


BASE 2 is ideal for dealing with conditions that can be ON or OFF. That is how a computer works. A "BIT" in a computer is like a switch, either ON (1) or OFF (0).

## And Furthermore ... exponent notation (a number with a superscript)

In BASE 10:
the right most digit represents how many 10 s to the 0th power $\left(10^{0}=1\right)$ there are. the next digit to the left represents how many 10 s to the 1 st power $\left(10^{1}=10\right)$ there are. the next digit to the left represents how many 10 s to the 2 nd power $\left(10^{2}=10 \times 10\right)$ there are. the next digit to the left represents how many 10s to the 3rd power ( $10^{3}=10 \times 10 \times 10$ ) there are. ... and so on.


| Exponent <br> Notation | $10^{3}$ | $10^{2}$ | $10^{1}$ | $10^{0}$ |
| :--- | :---: | :---: | :---: | :---: |
| Place <br> Value: | 1000 | 100 | 10 | 1 |
| How <br> Many: | 5 | 6 | 0 | 8 |

In BASE 2:
the right most symbol represents how many 2 s to the 0 th power $\left(2^{0}=1\right)$ there are. the next symbol to the left represents how many 2 s to the 1 st power $\left(2^{1=} 2\right)$ there are. the next symbol to the left represents how many 2 s to the 2 nd power ( $2^{2}=2 \times 2$ ) there are. the next symbol to the left represents how many 2 s to the 3rd power $\left(2^{3}=2 \times 2 \times 2\right)$ there are.


More Furthermore ... binary representations (BASE 2)
Here are some equivalent ways to represent the same value, in BASE 10 \& in BASE 2.

| BASE | BASE 2 | BASE 1 | - BASE 2 | BASE 10 = BASE 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 11 | 1011 | 21 | 10101 |  |
| 2 | 10 | 12 | 1100 | 22 | 10110 |  |
| 3 | 11 | 13 | 1101 | 23 | 10111 |  |
| 4 | 100 | 14 | 1110 | 24 | 11000 |  |
| 5 | 101 | 15 | 1111 | 25 | 11001 |  |
| 6 | 110 | 16 | 10000 | 26 | 11010 |  |
| 7 | 111 | 17 | 10001 | 27 | 11011 |  |
| 8 | 1000 | 18 | 10010 | 28 | 11100 |  |
| 9 | 1001 | 19 | 10011 | 29 | 11101 |  |
| 10 | 1010 | 20 | 10100 | 30 | 11110 | .. and so on. |

## HOW the trick works :

1. The Volunteer Chooses a Secret Number between 1 and 60.
2. The Volunteer Selects the Card(s) that contain the Secret Number.
3. The Magician adds the Upper Left numbers on the Selected Card(s).
4. The Magician announces the Secret Number.

The Upper Left numbers are 1, 2, 4, 8, 16, \& 32.
Which are the BASE 2 "Place Values":
2 to the Oth power =1 $1=2^{0}$ (a number to the 0th power is equal to 1 )
2 to the 1 st power $=2 \quad 2=2^{1}$
2 to the 2 nd power $=4 \quad 2 \times 2=2^{2}$
2 to the 3 rd power $=8 \quad 2 \times 2 \times 2=2^{3}$
2 to the 4 th power $=16 \quad 2 \times 2 \times 2 \times 2=2^{4}$
2 to the 5th power $=32 \quad 2 \times 2 \times 2 \times 2 \times 2=2^{5}$

## WHY the trick works :

| Power of 2 | Calculation | Value |
| :---: | :---: | :---: |
| $2^{0}$ |  | 1 |
| $2^{1}$ | 2 | 2 |
| $2^{2}$ | 2 * 2 | 4 |
| $2^{3}$ | 2*2*2 | 8 |
| $2^{4}$ | 2*2 * 2 * 2 | 16 |
| $2^{5}$ | 2*2*2*2*2 | 32 |
| $2^{6}$ | 2*2*2*2*2 *2 | 64 |
| $2^{7}$ | 2*2*2*2*2 *2 * 2 | 128 |

Look at the table on the next pages and notice what numbers are printed on each card:
All Numbers on the YELLOW card ( $2^{0}$ ) have the right most symbol set to YES.
All Numbers on the GREEN card ( $2^{1}$ ) have the next symbol to the left set to YES.
All Numbers on the RED card ( $2^{2}$ ) have the next symbol to the left set to YES.
All Numbers on the BROWN card ( $2^{3}$ ) have the next symbol to the left set to YES.
All Numbers on the PINK card ( $2^{4}$ ) have the next symbol to the left set to YES.
All Numbers on the BLUE card ( $2^{5}$ ) have the next symbol to the left set to YES.

## Here is an Example:

Let's say your secret number is 20. - $\mathbf{2 0}_{10}$ equals $\mathbf{1 0 1 0 0}_{2}$.
The number 20 appears only on the RED and PINK cards.
The upper-left number on the RED card is 4 , which is the RED card PLACE VALUE.
The upper-left number on the PINK card is 16, which is the PINK card PLACE VALUE. If we add 4 to 16 , we get $20=$ your "secret number"!
The "magic" is that the selected cards "spell out" the secret number in Binary language.

| SECRET <br> Number | PLACE VALUE ---> | $\begin{gathered} 32 \\ \left(2^{5}\right) \end{gathered}$ | $\begin{gathered} 16 \\ \left(2^{4}\right) \end{gathered}$ | $\begin{gathered} 8 \\ \left(2^{3}\right) \end{gathered}$ | $\begin{gathered} 4 \\ \left(2^{2}\right) \end{gathered}$ | $\begin{gathered} 2 \\ \left(\mathbf{2}^{1}\right) \end{gathered}$ | $\begin{gathered} 1 \\ \left(2^{0}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DECIMAL | BINARY | Blue | Pink | Brown | Red | Green | Yellow |
| 1 | 1 |  |  |  |  |  | YES |
| 2 | 10 |  |  |  |  | YES |  |
| 3 | 11 |  |  |  |  | YES | YES |
| 4 | 100 |  |  |  | YES |  |  |
| 5 | 101 |  |  |  | YES |  | YES |
| 6 | 110 |  |  |  | YES | YES |  |
| 7 | 111 |  |  |  | YES | YES | YES |
| 8 | 1000 |  |  | YES |  |  |  |
| 9 | 1001 |  |  | YES |  |  | YES |
| 10 | 1010 |  |  | YES |  | YES |  |
| 11 | 1011 |  |  | YES |  | YES | YES |
| 12 | 1100 |  |  | YES | YES |  |  |
| 13 | 1101 |  |  | YES | YES |  | YES |
| 14 | 1110 |  |  | YES | YES | YES |  |
| 15 | 1111 |  |  | YES | YES | YES | YES |
| 16 | 10000 |  | YES |  |  |  |  |
| 17 | 10001 |  | YES |  |  |  | YES |
| 18 | 10010 |  | YES |  |  | YES |  |
| 19 | 10011 |  | YES |  |  | YES | YES |
| 20 | 10100 |  | YES |  | YES |  |  |
| 21 | 10101 |  | YES |  | YES |  | YES |
| 22 | 10110 |  | YES |  | YES | YES |  |
| 23 | 10111 |  | YES |  | YES | YES | YES |
| 24 | 11000 |  | YES | YES |  |  |  |
| 25 | 11001 |  | YES | YES |  |  | YES |
| 26 | 11010 |  | YES | YES |  | YES |  |
| 27 | 11011 |  | YES | YES |  | YES | YES |
| 28 | 11100 |  | YES | YES | YES |  |  |
| 29 | 11101 |  | YES | YES | YES |  | YES |
| 30 | 11110 |  | YES | YES | YES | YES |  |
| 31 | 11111 |  | YES | YES | YES | YES | YES |


| 32 | 100000 | YES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | 100001 | YES |  |  |  |  | YES |
| 34 | 100010 | YES |  |  |  | YES |  |
| 35 | 100011 | YES |  |  |  | YES | YES |
| 36 | 100100 | YES |  |  | YES |  |  |
| 37 | 100101 | YES |  |  | YES |  | YES |
| 38 | 100110 | YES |  |  | YES | YES |  |
| 39 | 100111 | YES |  |  | YES | YES | YES |
| 40 | 101000 | YES |  | YES |  |  |  |
| 41 | 101001 | YES |  | YES |  |  | YES |
| 42 | 101010 | YES |  | YES |  | YES |  |
| 43 | 101011 | YES |  | YES |  | YES | YES |
| 44 | 101100 | YES |  | YES | YES |  |  |
| 45 | 101101 | YES |  | YES | YES |  | YES |
| 46 | 101110 | YES |  | YES | YES | YES |  |
| 47 | 101111 | YES |  | YES | YES | YES | YES |
| 48 | 110000 | YES | YES |  |  |  |  |
| 49 | 110001 | YES | YES |  |  |  | YES |
| 50 | 110010 | YES | YES |  |  | YES |  |
| 51 | 110011 | YES | YES |  |  | YES | YES |
| 52 | 110100 | YES | YES |  | YES |  |  |
| 53 | 110101 | YES | YES |  | YES |  | YES |
| 54 | 110110 | YES | YES |  | YES | YES |  |
| 55 | 110111 | YES | YES |  | YES | YES | YES |
| 56 | 111000 | YES | YES | YES |  |  |  |
| 57 | 111001 | YES | YES | YES |  |  | YES |
| 58 | 111010 | YES | YES | YES |  | YES |  |
| 59 | 111011 | YES | YES | YES |  | YES | YES |
| 60 | 111100 | YES | YES | YES | YES |  |  |
| The Cards contain only the "YES" numbers... |  |  |  |  |  |  |  |

I hope that you will think about this (with somebody else or alone) and recognize the beauty of the mathematics that this silly trick is based upon.

If you did ... the reward can be life changing!
If you didn't ... there will be many more opportunities!

## Parting Thoughts:

The Book/Video/Radio Program "The Hitchhiker's Guide to the Galaxy; The Restaurant at the End of the Universe" suggests that 42 is the ultimate answer, and that the ultimate question is:
"What do you get if you multiply six by nine?".
This is valid mathematics if you are doing math in BASE 13.
42 in BASE 13, is the same as 54 in BASE $10\left(42_{13}=54_{10}\right)$ :

$$
(4 \times 13+2 \times 1)=54=(5 \times 10+4 \times 1)=6 \times 9 .
$$



BASE 10
BASE 13


Perhaps, suggesting that "Enlightenment" will be achieved if we count in the correct base! What fun!

For More Exciting Information See:
Go to jorgezimmerman.org and select 'Magic Cards, Explained' for hyperlinks and video.
https://en.wikipedia.org/wiki/Decimal - for more about Decimal (Base 10)
https://en.wikipedia.org/wiki/Binary number - for more about Binary (Base 2)
https://en.wikipedia.org/wiki/
List of numeral systems\#Standard positional numeral systems - for more more
https://en.wikipedia.org/wiki/The Hitchhiker\%27s Guide to the Galaxy

- for less, but a good laugh!

